

8A: $6 \cdot x^\alpha, y^\beta, 2^k \cdot z^\gamma, 3^l$

$x = 5, y = 7, z = 11$: If l is odd then both $2^k \cdot 11^\gamma$ and $2^k \cdot 11^\gamma + 2 = 3^l + 1 = 4 \cdot (3^{l-1} - 3^{l-2} + \dots + 1)$ would be divisible by 4. So l is even, and so is $l' = l/2$: if not then $6 \cdot 5^\alpha + 4 = 3^l + 1 = 3^{2l'} + 1 = 9^{l'} + 1 = 10 \cdot (9^{l'-1} - 9^{l'-2} + \dots + 1)$ would be divisible by 5. It follows that $2^k \cdot 11^\gamma = 3^l - 1 = 3^{4l''} - 1 = 81^{l''} - 1 = 80 \cdot (81^{l''-1} + \dots + 1)$ is divisible by 5, contradiction.

$x = 5, y = 11, z = 7$: $6 \cdot 5^\alpha = 11^\beta - 1 = 10 \cdot (11^{\beta-1} + \dots + 1)$ yields $3 \cdot 5^{\alpha-1} = 11^{\beta-1} + \dots + 1$: β must be odd. It follows that $2^k \cdot 7^\gamma = 11^\beta + 1 = 12 \cdot (11^{\beta-1} - 11^{\beta-2} + \dots + 1)$ is divisible by 3, contradiction.

$x = 7, y = 5, z = 11$: $6 \cdot 7^\alpha = 5^\beta - 1 = 4 \cdot (5^{\beta-1} + \dots + 1)$ is divisible by 2^2 , contradiction.

$x = 7, y = 11, z = 5$: $6 \cdot 7^\alpha = 11^\beta - 1 = 10 \cdot (11^{\beta-1} + \dots + 1)$ is divisible by 5, contradiction.

$x = 11, y = 5, z = 7$: $6 \cdot 11^\alpha = 5^\beta - 1 = 4 \cdot (5^{\beta-1} + \dots + 1)$ is divisible by 2^2 , contradiction.

$x = 11, y = 7, z = 5$: Both $6 \cdot 11^\alpha + 2 = 2^k \cdot 5^\gamma$ and $6 \cdot 11^\alpha - 6 = 6 \cdot (11^\alpha - 1) = 6 \cdot 10 \cdot (11^{\alpha-1} + \dots + 1)$ are divisible by 5, contradiction.