

6A: $3 \cdot x^\alpha$, $2^k \cdot y^\beta$, z^γ , $2 \cdot 3^l$

$x = 5, y = 7, z = 11$: γ must be even, otherwise $2 \cdot 3^l = 11^\gamma + 1 = 12 \cdot (11^{\gamma-1} - 11^{\gamma-2} + \dots + 1)$ would be divisible by 2^2 . But then $2^k \cdot 7^\beta = 11^\gamma - 1 = 11^{2\gamma} - 1 = 121^\gamma - 1 = 120 \cdot (121^{\gamma-1} + \dots + 1)$ would be divisible by 3 and 5, contradiction.

$x = 5, y = 11, z = 7$: $2^k \cdot 11^\beta = 7^\gamma - 1 = 6 \cdot (7^{\gamma-1} + \dots + 1)$ is divisible by 3, contradiction.

$x = 7, y = 5, z = 11$: Both $2 \cdot 3^l$ and $2 \cdot 3^l - 6 = 3 \cdot 7^\alpha - 3 = 3 \cdot (7^\alpha - 1) = 3 \cdot 6 \cdot (7^{\alpha-1} + \dots + 1)$ are divisible by 9, contradiction. (We may and do assume $l \geq 2$.)

$x = 7, y = 11, z = 5$: as in case $x = 7$ above.

$x = 11, y = 5, z = 7$: $2^k \cdot 5^\beta - 4 = 3 \cdot 11^\alpha - 3 = 3 \cdot (11^\alpha - 1) = 3 \cdot 10 \cdot (11^{\alpha-1} + \dots + 1)$ is divisible by 5, contradiction.

$x = 11, y = 7, z = 5$: α must be even, otherwise $2 \cdot 3^l = 3 \cdot 11^\alpha + 3 = 3 \cdot (11^\alpha + 1) = 3 \cdot 12 \cdot (11^{\alpha-1} - 11^{\alpha-2} + \dots + 1)$ would be divisible by 2^2 . But then both $2 \cdot 3^l$ and $2 \cdot 3^l - 6 = 3 \cdot 11^\alpha - 3 = 3 \cdot (11^\alpha - 1) = 3 \cdot (11^{2\alpha'} - 1) = 3 \cdot (121^{\alpha'} - 1) = 3 \cdot 120 \cdot (121^{\alpha'-1} + \dots + 1)$ would be divisible by 9, contradiction. (Again we may and do assume $l \geq 2$.)