

5A: $3 \cdot x^\alpha, 2 \cdot y^\beta, z^\gamma, 2^k \cdot 3^l$

$x = 5, y = 7, z = 11$: $2 \cdot 7^\beta = 11^\gamma - 1 = 10 \cdot (11^{\gamma-1} + \dots + 1)$ is divisible by 5, contradiction.

$x = 5, y = 11, z = 7$: $2 \cdot 11^\beta = 7^\gamma - 1 = 6 \cdot (7^{\gamma-1} + \dots + 1)$ is divisible by 3, contradiction.

$x = 7, y = 5, z = 11$: Both $3 \cdot 7^\alpha + 3 = 2^k \cdot 3^l$ and $3 \cdot 7^\alpha - 3 = 3 \cdot (7^\alpha - 1) = 3 \cdot 6 \cdot (7^{\alpha-1} + \dots + 1)$ are divisible by 9, contradiction. (We may and do assume $l \geq 2$: indeed $l = 1$ implies $7^\alpha + 1 = 2^k$, something that might only happen for $\alpha = 1$ and $k = 3$, leading to $2 \cdot 5^\beta = 22$ and $11^\gamma = 23$.)

$x = 7, y = 11, z = 5$: $2 \cdot 11^\beta = 5^\gamma - 1 = 4 \cdot (5^{\gamma-1} + \dots + 1)$ is divisible by 2^2 , contradiction.

$x = 11, y = 5, z = 7$: $2 \cdot 5^\beta = 7^\gamma - 1 = 6 \cdot (7^{\gamma-1} + \dots + 1)$ is divisible by 3, contradiction.

$x = 11, y = 7, z = 5$: $2 \cdot 7^\beta = 5^\beta - 1 = 4 \cdot (5^{\beta-1} + \dots + 1)$ is divisible by 2^2 , contradiction.