

3A: $x^\alpha, 2 \cdot 3^l, y^\beta, 2^k \cdot z^\gamma$

$x = 5, y = 7, z = 11$: We may and do assume $\beta \geq 2$ and $l \geq 2$, so that $7^\beta = 2 \cdot 3^l + 1$ implies that β is divisible by 3 via $(2 \cdot 3 + 1)^\beta = 2 \cdot 3^l + 1$ and $9 \cdot M + 6 \cdot \beta = 2 \cdot 3^l$. But then $2 \cdot 3^l = 7^\beta - 1 = 7^{3\beta'} - 1 = 343^{\beta'} - 1 = 342 \cdot (343^{\beta'-1} + \dots + 1)$ would be divisible by $2 \cdot 3^2 \cdot 19$, contradiction.

$x = 5, y = 11, z = 7$: $2 \cdot 3^l = 11^\beta - 1 = 10 \cdot (11^{\beta-1} + \dots + 1)$ is divisible by 5, contradiction.

$x = 7, y = 5, z = 11$: $2 \cdot 3^l = 5^\beta - 1 = 4 \cdot (5^{\beta-1} + \dots + 1)$ is divisible by 2^2 , contradiction.

$x = 7, y = 11, z = 5$: $2 \cdot 3^l - 2 = 7^\alpha - 1 = 6 \cdot (7^{\alpha-1} + \dots + 1)$ is divisible by 3, contradiction.

$x = 11, y = 5, z = 7$: $5^\beta - 3 = 11^\alpha - 1 = 10 \cdot (11^{\alpha-1} + \dots + 1)$ is divisible by 5, contradiction.

$x = 11, y = 7, z = 5$: $2^k \cdot 5^\gamma - 4 = 11^\alpha - 1 = 10 \cdot (11^{\alpha-1} + \dots + 1)$ is divisible by 5, contradiction.